**LECTURE ASSIGNMENT 2**

Consider vibration of a rectangular membrane of side length , density , thickness , and tightening  (force per unit length). If the edges are fixed, find the angular velocity of the free vibrations using the Finite Element Method on a regular grid of points . Consider the mode, which is reflection symmetric with respect to the lines through the center point (figure).

*x*

*L*

*y*

*L*

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In a time-dependent membrane problem without external forces, the equations given by the Finite Element Method on regular grid of spacing  and piecewise linear approximation on a regular triangle division are



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Initial conditions are not needed in modal analysis. In the present problem, displacement vanishes at the boundary points and, due to the symmetry, displacements at the interior points should be equal. Denoting the common value by



all equations for the interior points boil down to

 where .

Therefore, the frequency of the assumed mode shape

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